Problem. Assume O is the midpoint for both segments $[AB]$ and $[CD]$. Prove that $AC = BD$.

Since O is the midpoint for both segments $[AB]$ and $[CD]$, we have $OA = OB$ and $OC = OD$

Now,

$$AC = OA + OC = OB + OD = BD,$$

hence the result.